

**This is an explanation of the question N. 3 that we got on Friday 11/11.**

**Question:** A wire of gold is 1.00km long and has diameter of 1.00mm. The resistivity of gold is  $22.4\text{n}\Omega\text{m}$ . What is the resistance of the wire?

**Explanation:** So, first we may start by looking at what we already know. We know the *length*, the *diameter*, and the *resistivity* of wire. Look at the table below:

Length	$1.00\text{ km} = 1.00 \times 10^3$
Diameter	$1.00\text{ mm} = 1.00 \times 10^{-3}$
Resistivity	$22.4\text{ n}\Omega\text{m} = 22.4 \times 10^{-9}$

So, as chapter 1 says, 1.00 km is the same as  $1.00 \times \text{km}$ . "km" is only a variable. It is as "x" (10x). In our equation, it is important to include these variables.

To write our equation, we have to know which formulas we will use. At our formulae booklet you will find  $R = \rho \frac{l}{A}$ . We also need a formula to calculate the area of the wire.  $A = \pi r^2$

So, here is the answer:

$$R = \rho \frac{l}{A} = 22.4\text{ n}\Omega\text{m} \times \frac{1.00\text{ km}}{\pi \times 0.5\text{ mm}^2} = 22.4 \times 10^{-9} \times \frac{1.00 \times 10^3}{\pi \times (0.5 \times 10^{-3})^2}$$

1. As we know, radius is equal to diameter divided by two.
2. Once again, *mm* counts as a variable. Therefore, it is in brackets.
3. To calculate this equation, use your calculator. To get resistance, write  
 $22.4 \times 10^{(-9)} \times (1.00 \times 10^3) \div (\pi \times (0.5 \times 10^{(-3)})^2)$

The result should be "28.5205658". However, we only have 3 significant figures in our question, so the answer should be "28.5". The resistance is therefore 28.5Ω

**Improvement:**

As you might see, we have lot of numbers that actually could be crossed out. We can simplify the equation:

$$\begin{aligned} 22.4 \times 10^{-9} \times \frac{1.00 \times 10^3}{\pi \times (0.5 \times 10^{-3})^2} &= 22.4 \times \frac{10^{-9} \times 10^3}{\pi \times 0.5^2 \times 10^{-6}} = 22.4 \times \frac{10^{-6}}{\pi \times 0.5^2 \times 10^{-6}} = \\ &= 22.4 \times \frac{1}{\pi \times 0.25} = \frac{22.4}{0.25\pi} \end{aligned}$$

As you see, we do not need to write the whole thing as it was done in the previous example. Just simplify!